



New insights in the modelling of slope stability and avalanche sizes

J. Gaume(1), J. Schweizer(1), A. van Herwijnen(1), G. Chambon(2),
N. Eckert(2), M. Naaim(2)



(1) WSL Institute for Snow and Avalanche Research SLF, Davos, Switzerland



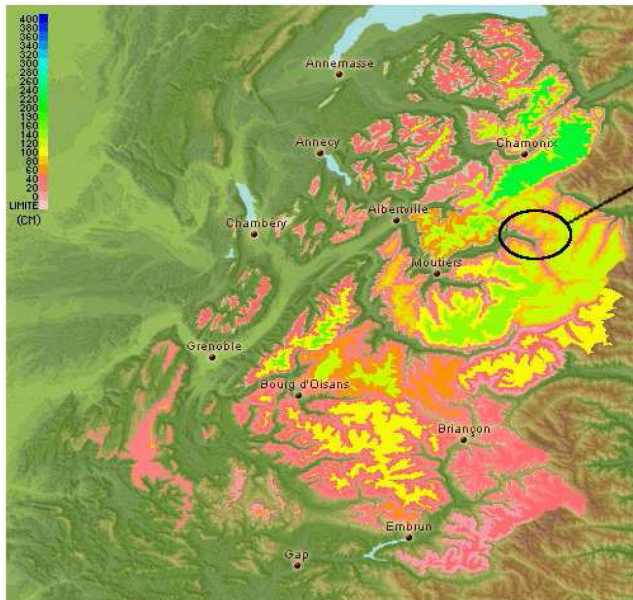
(2) IRSTEA, Grenoble, France

OSUG Snow workshop – 15/11/2013

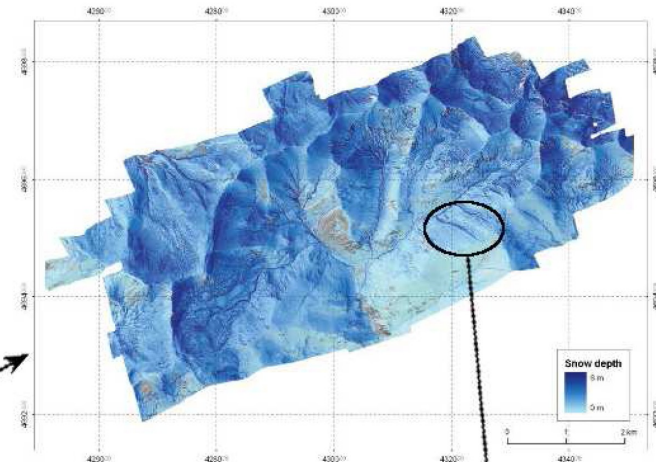


Context

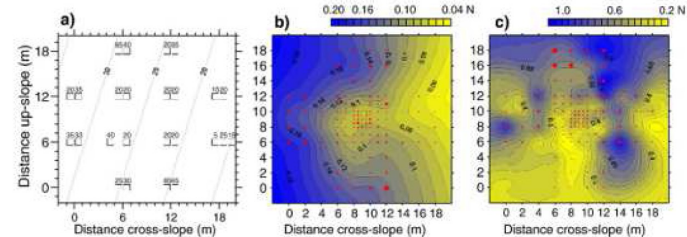
Complexity of avalanche forecasting due to a multi-scale spatial variability



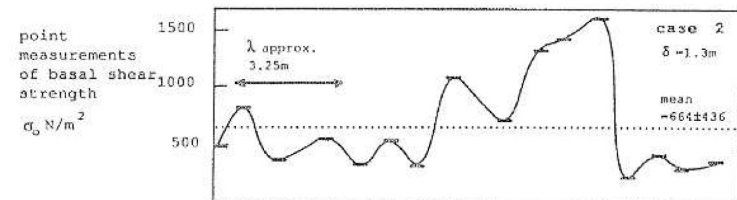
(c) Avalanches-net



From Banos et al 2011



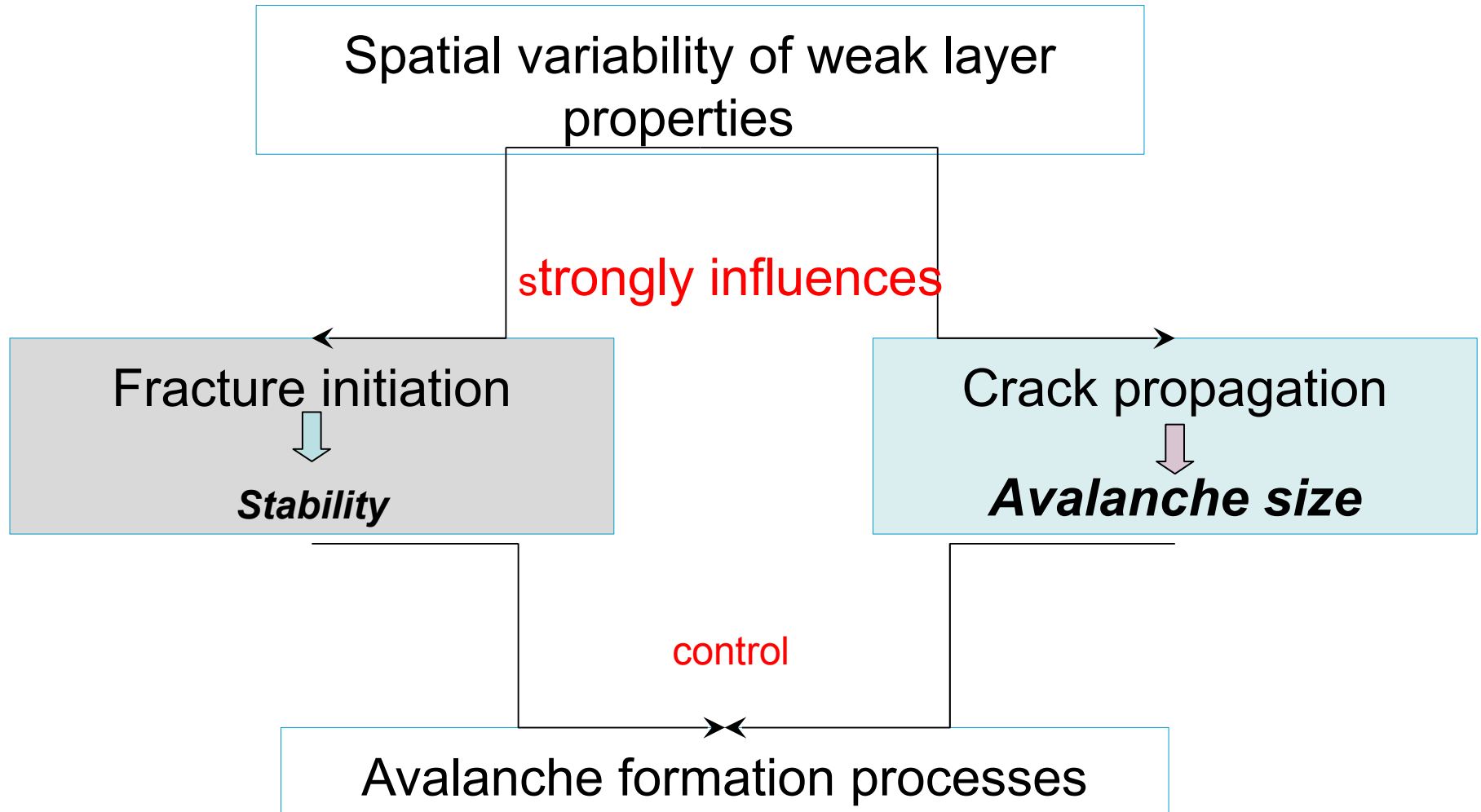
From Schweizer 2008



From Conway and Abrahamson 1988

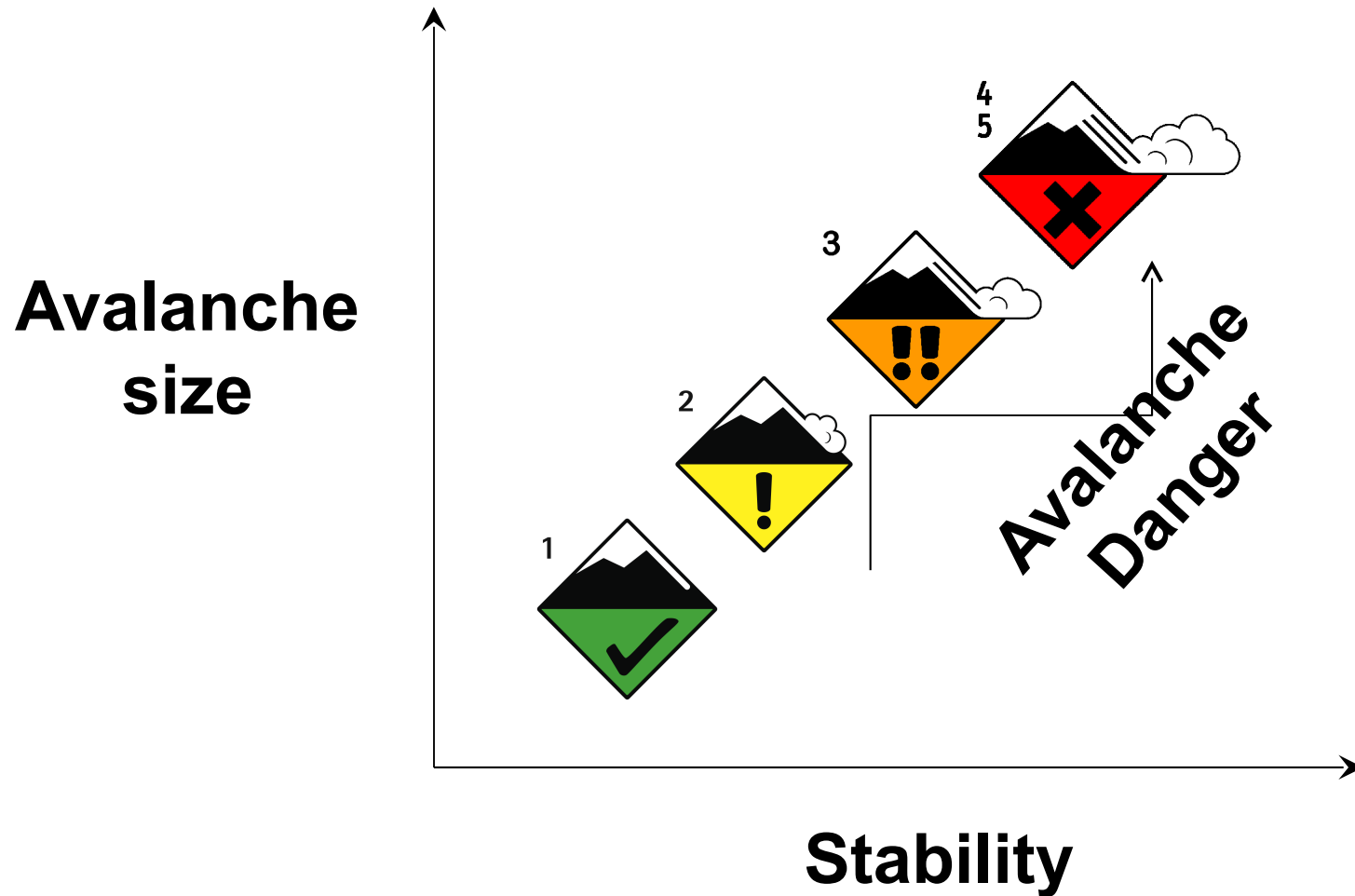
Context

Importance of spatial variability for avalanche formation



Context

Forecasting requires both stability and the avalanche size



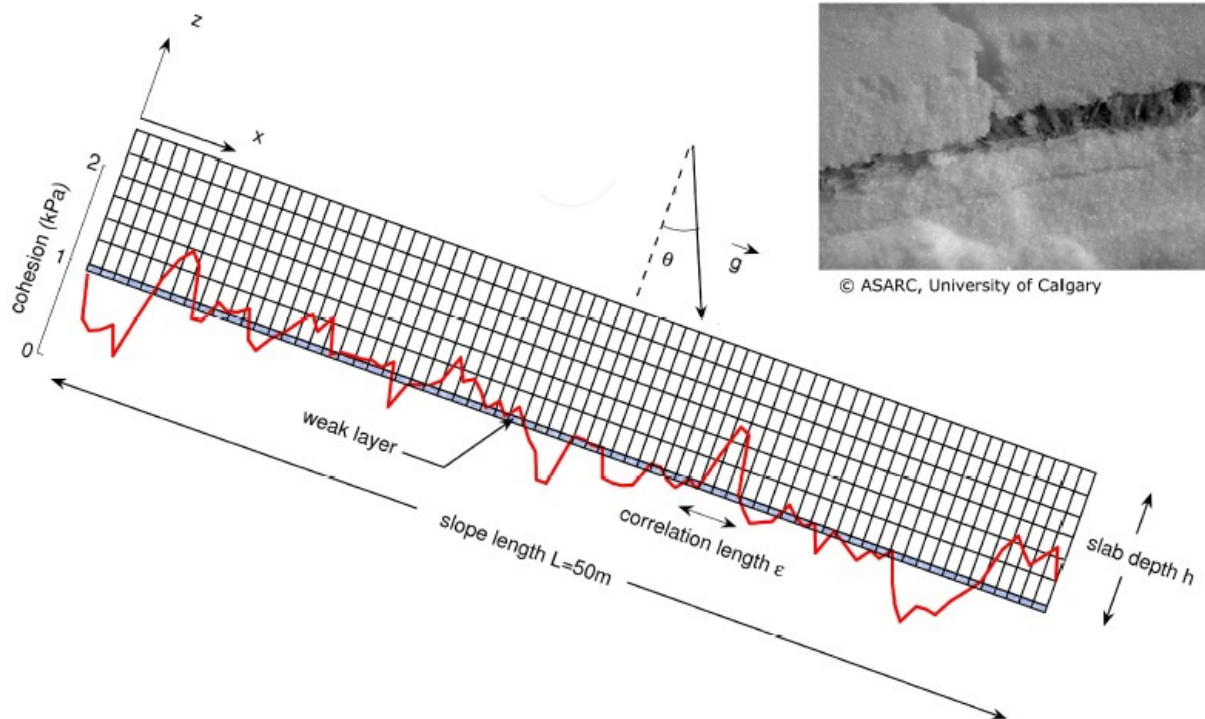
Objective and method

Objective

Spatial variability $\Rightarrow$? $\Rightarrow$ slope stability and avalanche size

Method

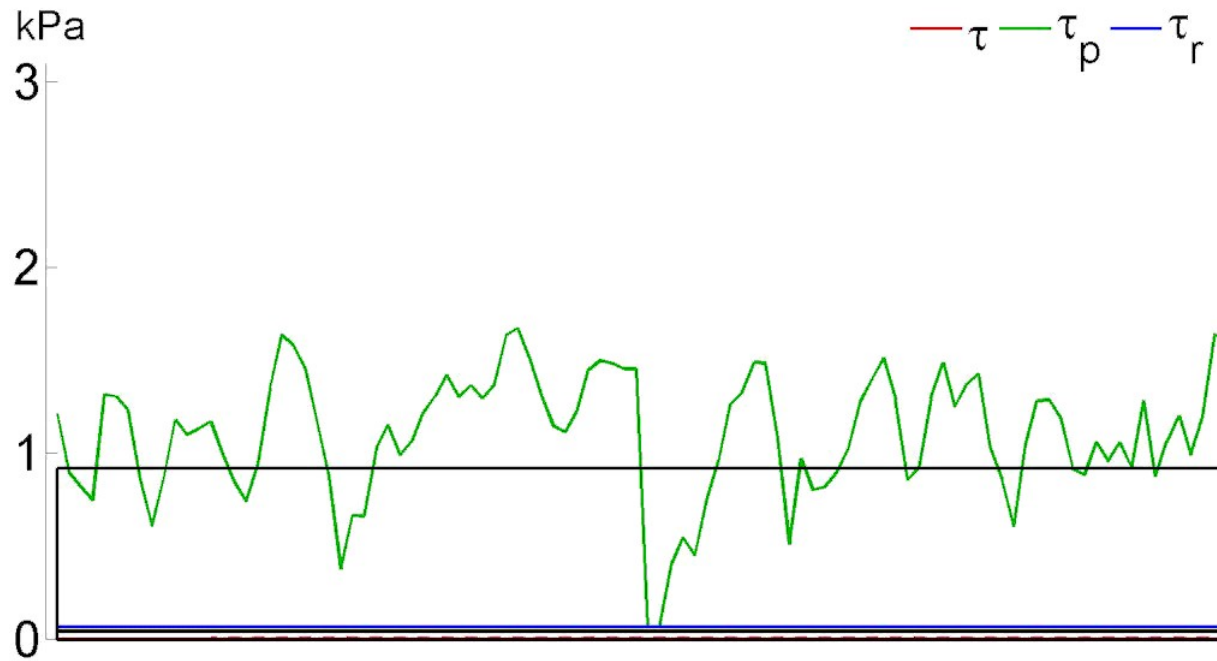
Mechanically-based statistical model of slab avalanche release
Gaume et al. (2012, 2013)



This model takes into account, in particular:

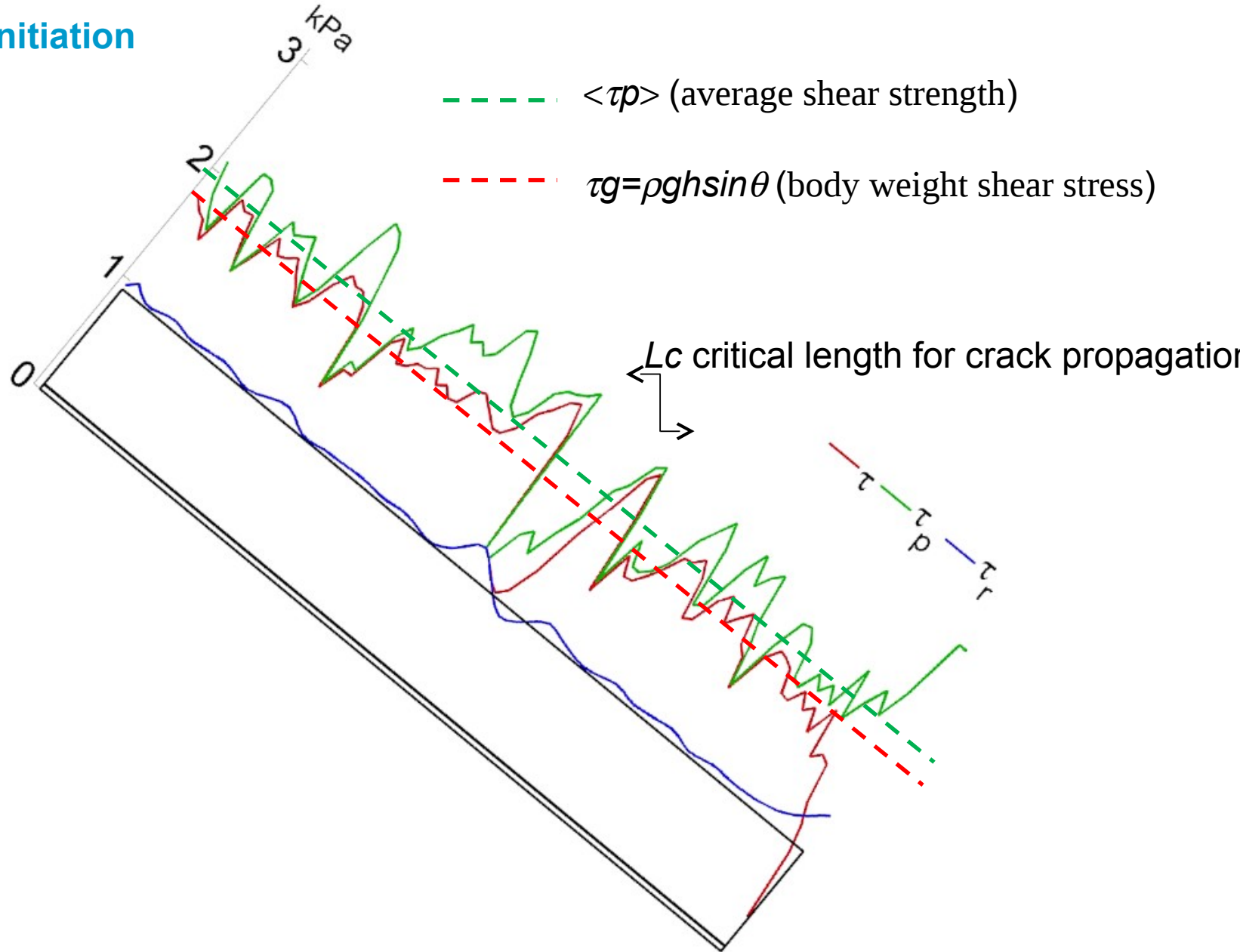
- (1) the spatial variations of WL mechanical properties (shear strength)
- (2) a shear quasi-brittle constitutive law for the WL
- (3) stress redistribution effects by elasticity of the slab

Illustration



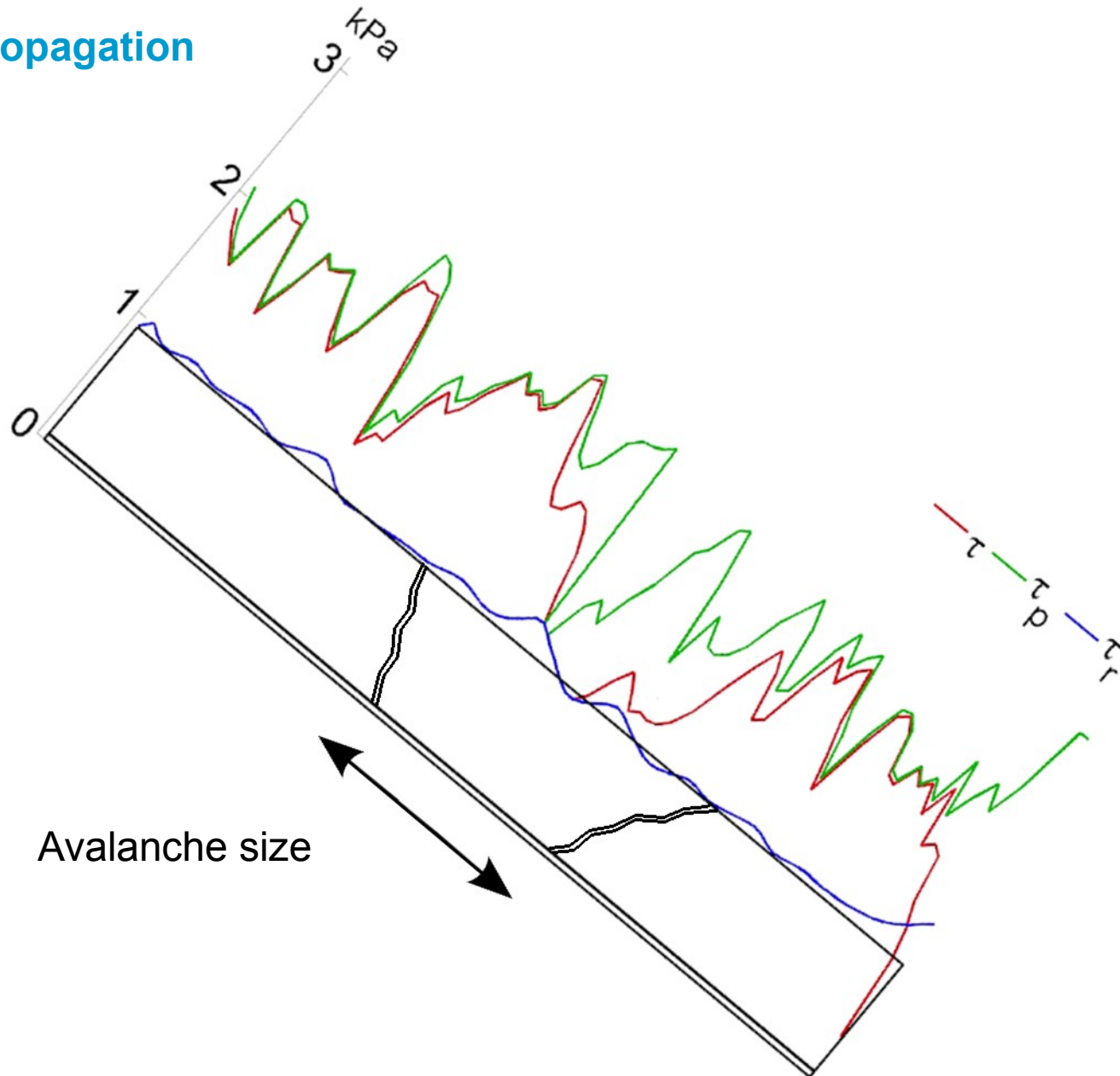
Illustration

Failure initiation



Illustration

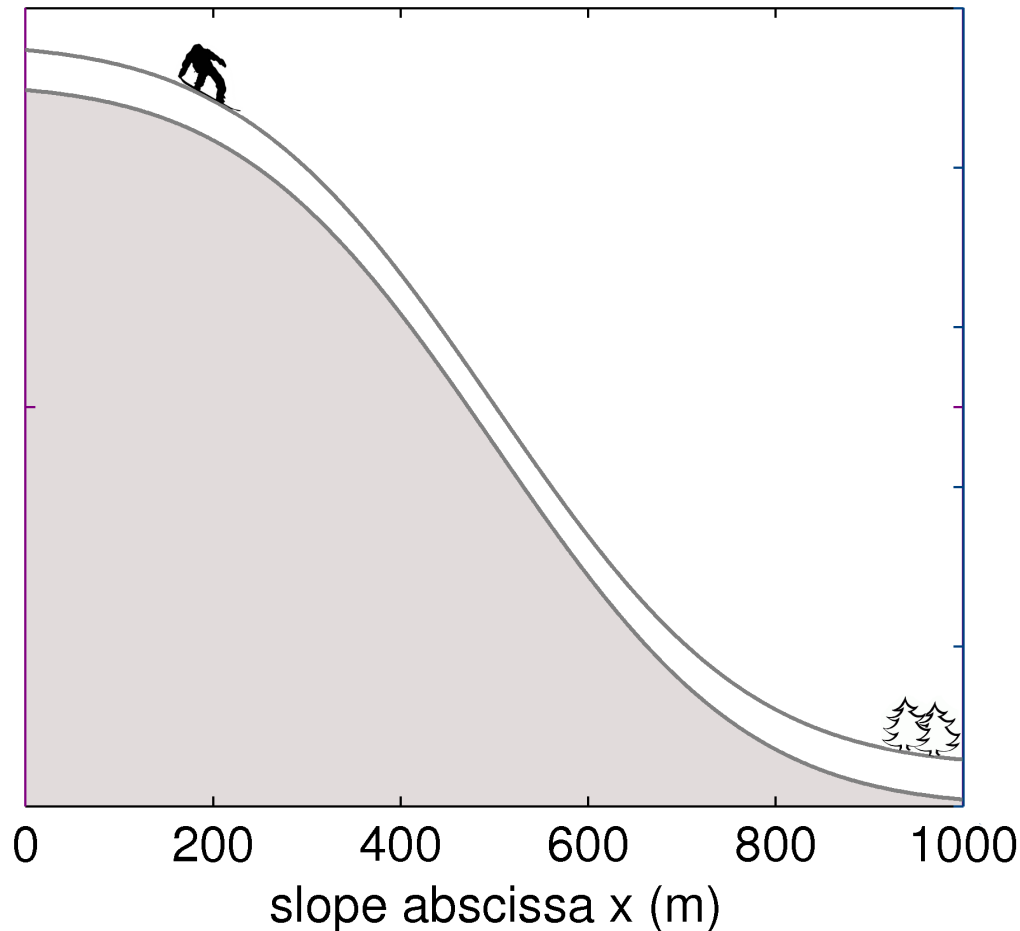
Crack propagation



Results

Slope stability evaluation

$hz=50\text{cm}$
 $\rho=250\text{kg/m}^3$
 $E=1\text{MPa}$
 $\tau_p=800\text{Pa}$

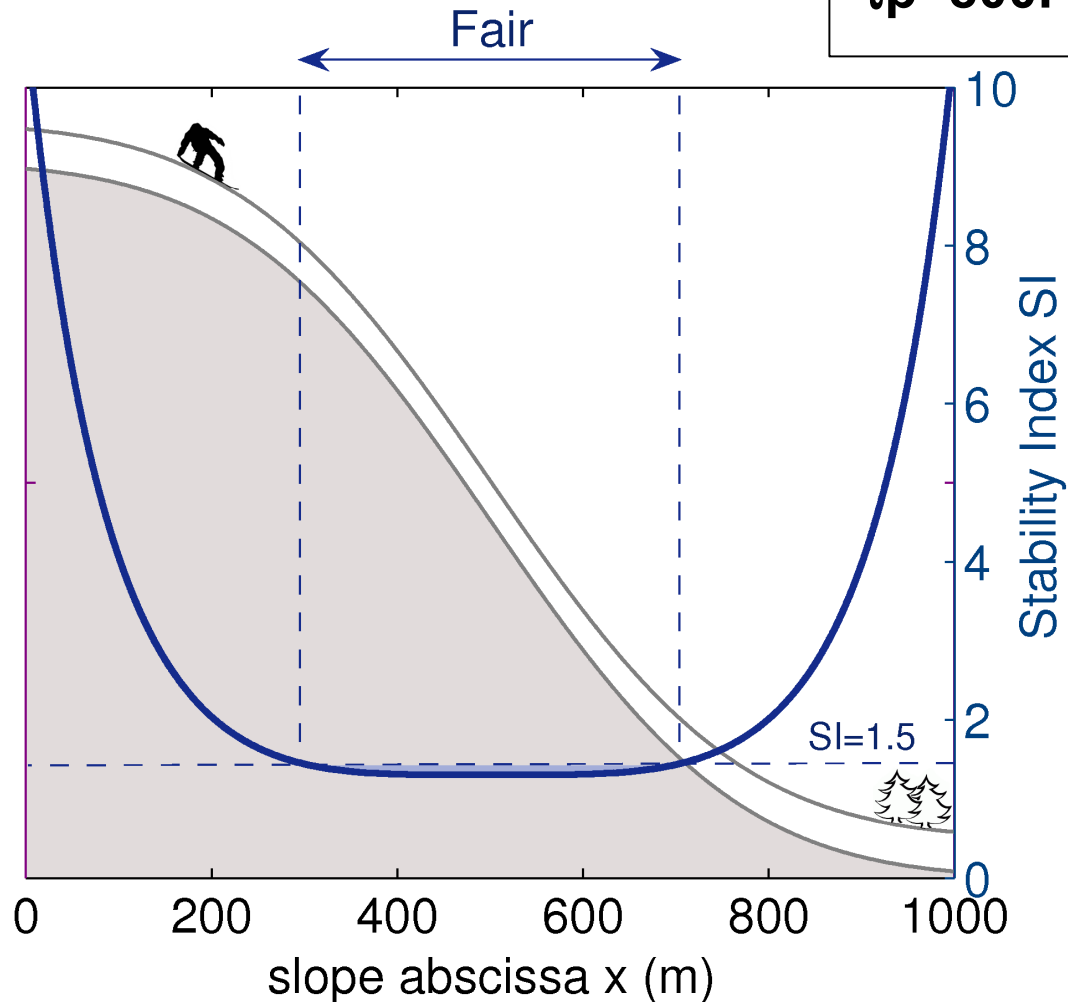


$$\begin{aligned} \text{Stability index } SI &= \frac{\text{shear strength}}{\text{shear stress}} \\ &= \frac{\tau_p}{\tau_{xz}} \end{aligned}$$

Results

Slope stability evaluation

$hz=50\text{cm}$
 $\rho=250\text{kg/m}^3$
 $E=1\text{MPa}$
 $\tau_p=800\text{Pa}$



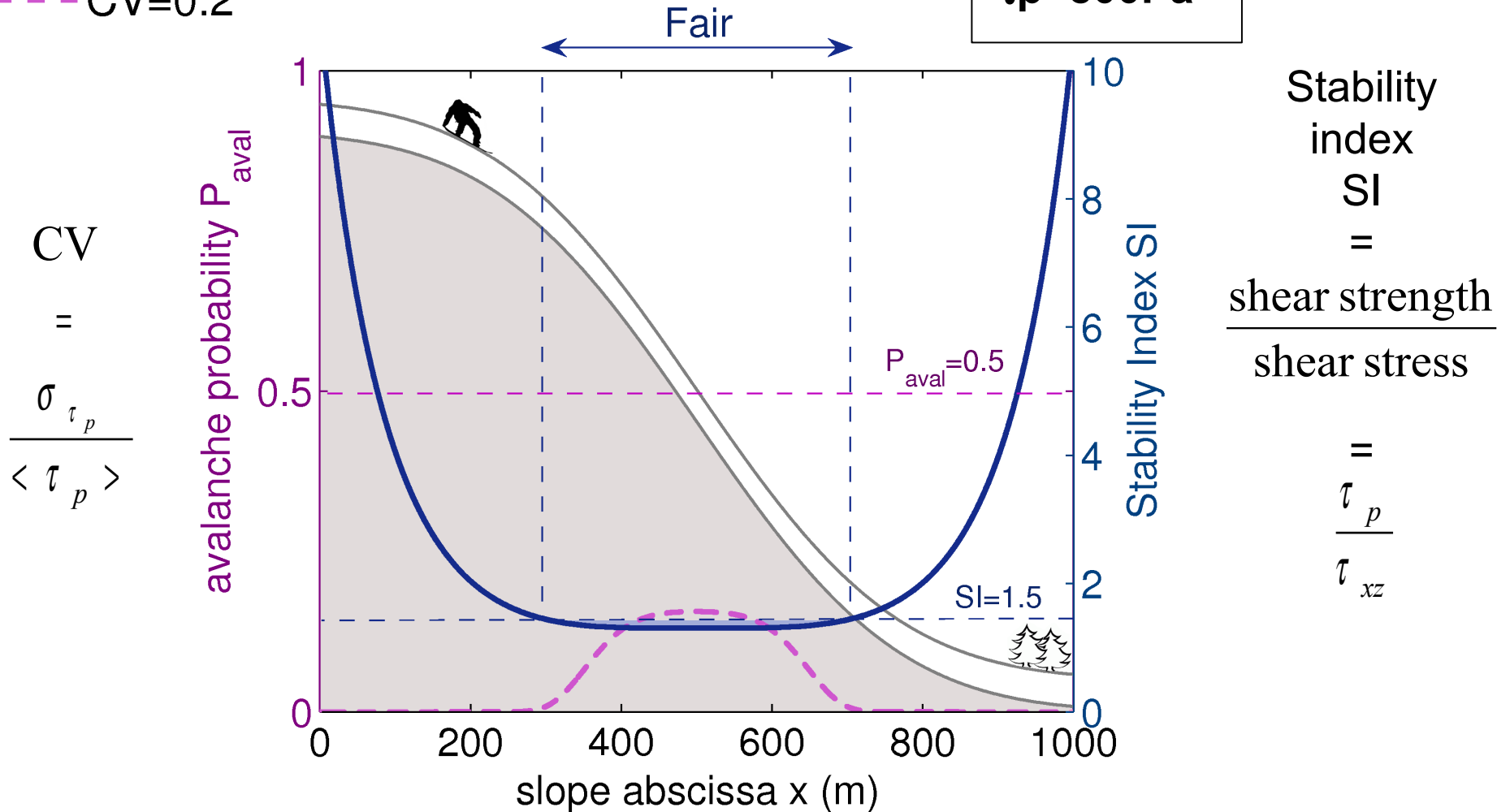
$$\begin{aligned}\text{Stability index } SI &= \frac{\text{shear strength}}{\text{shear stress}} \\ &= \frac{\tau_p}{\tau_{xz}}\end{aligned}$$

Results

Slope stability evaluation

-- CV=0.2

$hz=50\text{cm}$
 $\rho=250\text{kg/m}^3$
 $E=1\text{MPa}$
 $\tau_p=800\text{Pa}$



Results

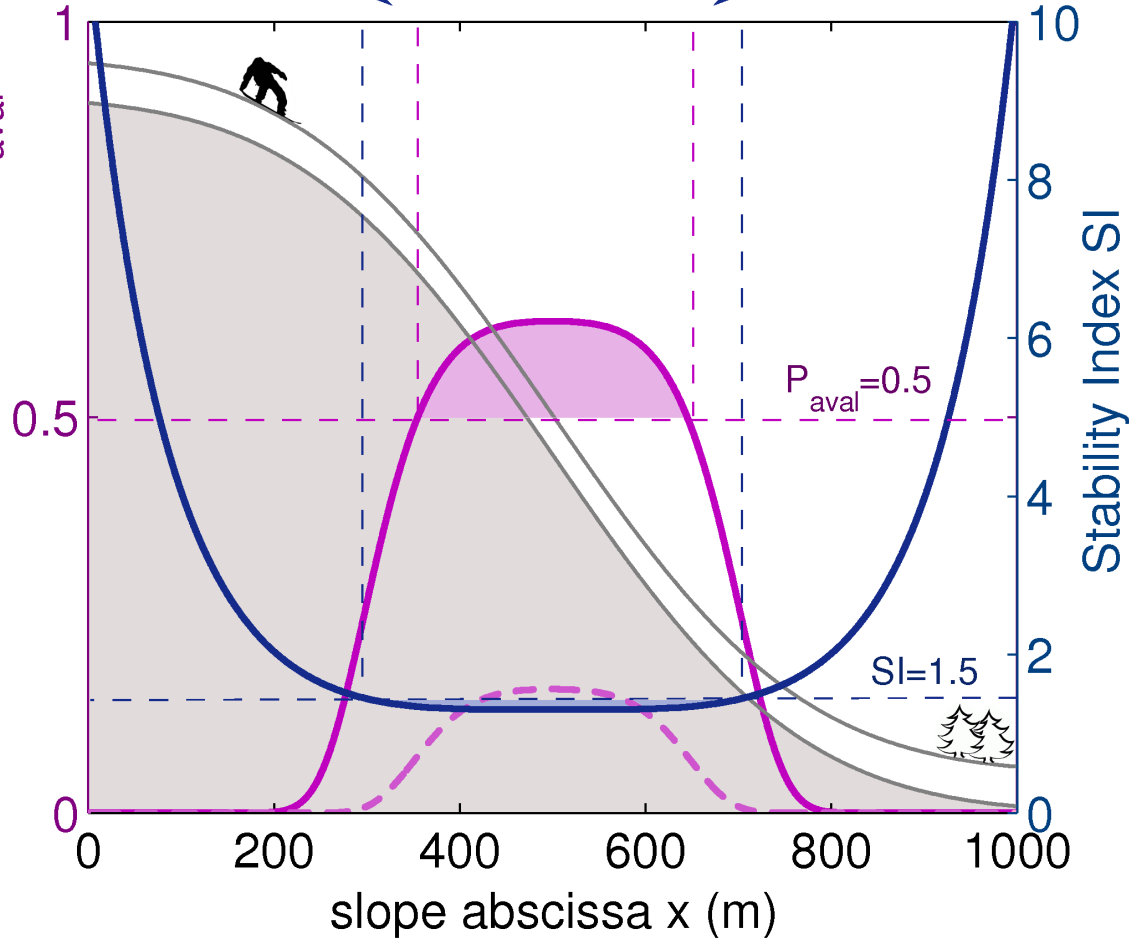
Slope stability evaluation

-- CV=0.2

— CV=0.3

$$CV = \frac{\sigma_{\tau_p}}{\langle \tau_p \rangle}$$

avalanche probability P_{aval}



$hz=50\text{cm}$
 $\rho=250\text{kg/m}^3$
 $E=1\text{MPa}$
 $\tau_p=800\text{Pa}$

$$\begin{aligned} \text{Stability index } SI &= \frac{\text{shear strength}}{\text{shear stress}} \\ &= \frac{\tau_p}{\tau_{xz}} \end{aligned}$$

Results

Slope stability evaluation

-- CV=0.2

— CV=0.3

$h_z=50\text{cm}$

$\rho=250\text{kg/m}^3$

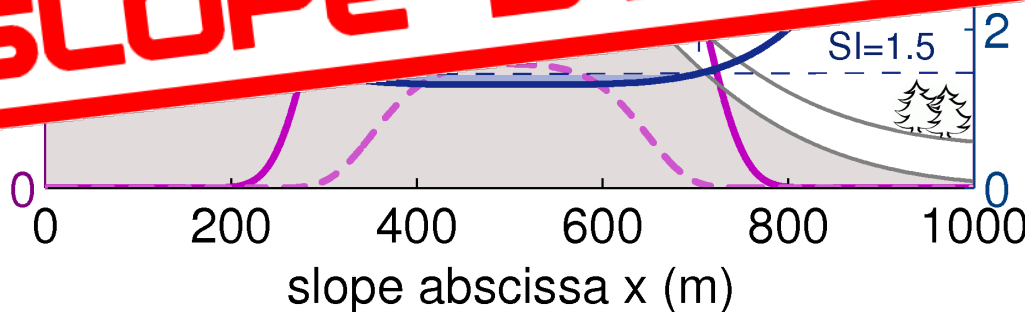
$E=1\text{MPa}$

$\tau_p=800\text{Pa}$

Unstable

Fair

**SPATIAL VARIABILITY:
KNOCK-DOWN EFFECT
ON
SLOPE STABILITY**



Slope stability evaluation

— CV=0.3

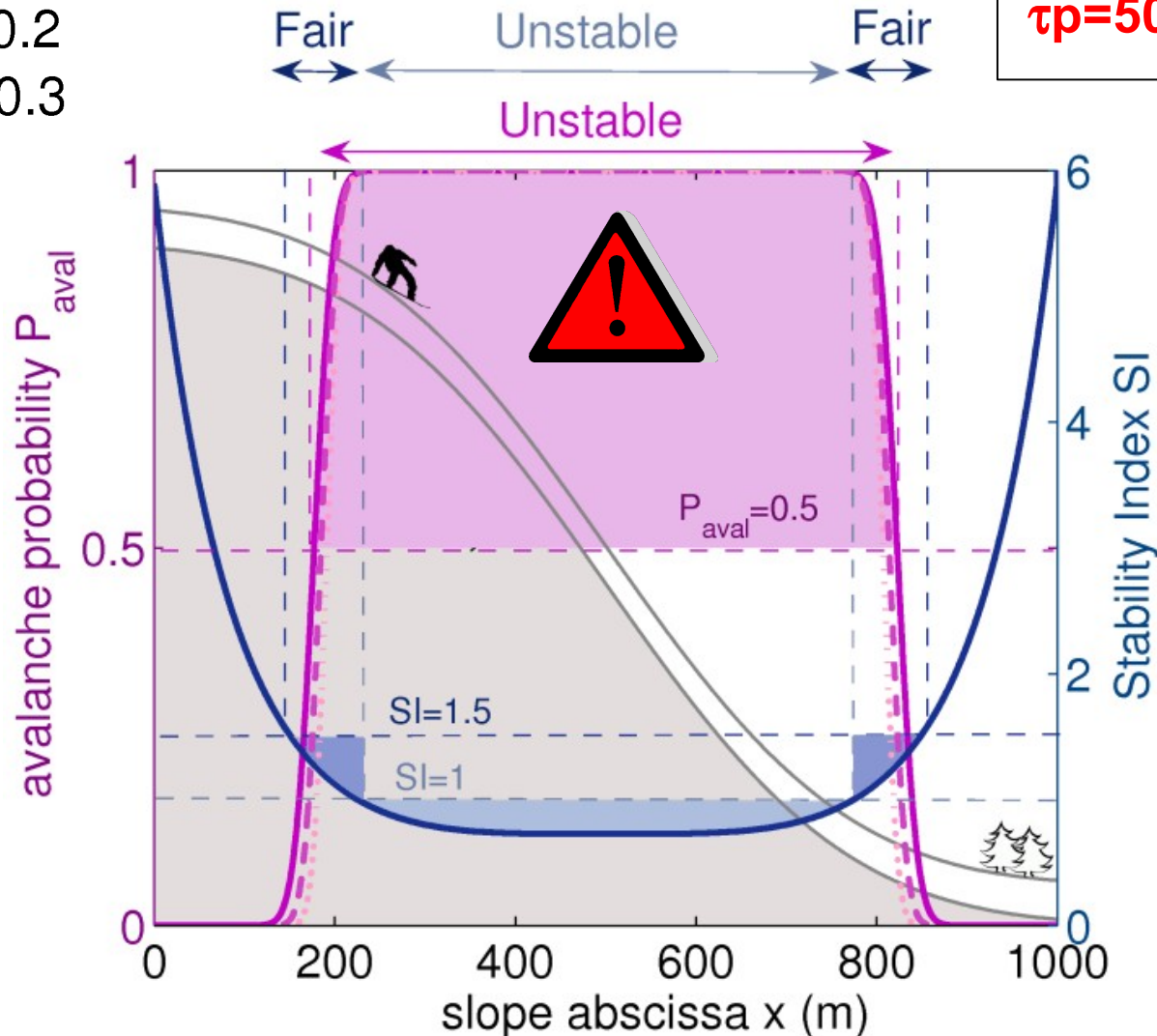
$$\frac{CV}{\sigma_{\tau_p}} = \frac{\sigma_{\tau_p}}{\langle \tau_p \rangle}$$

$h_z = 50 \text{ cm}$
 $\rho = 250 \text{ kg/m}^3$
 $E = 1 \text{ MPa}$
 $\tau_p = 500 \text{ Pa}$

Stability index SI

$$\frac{\text{shear strength}}{\text{shear stress}}$$

$$\frac{\tau_p}{\tau_{xz}}$$



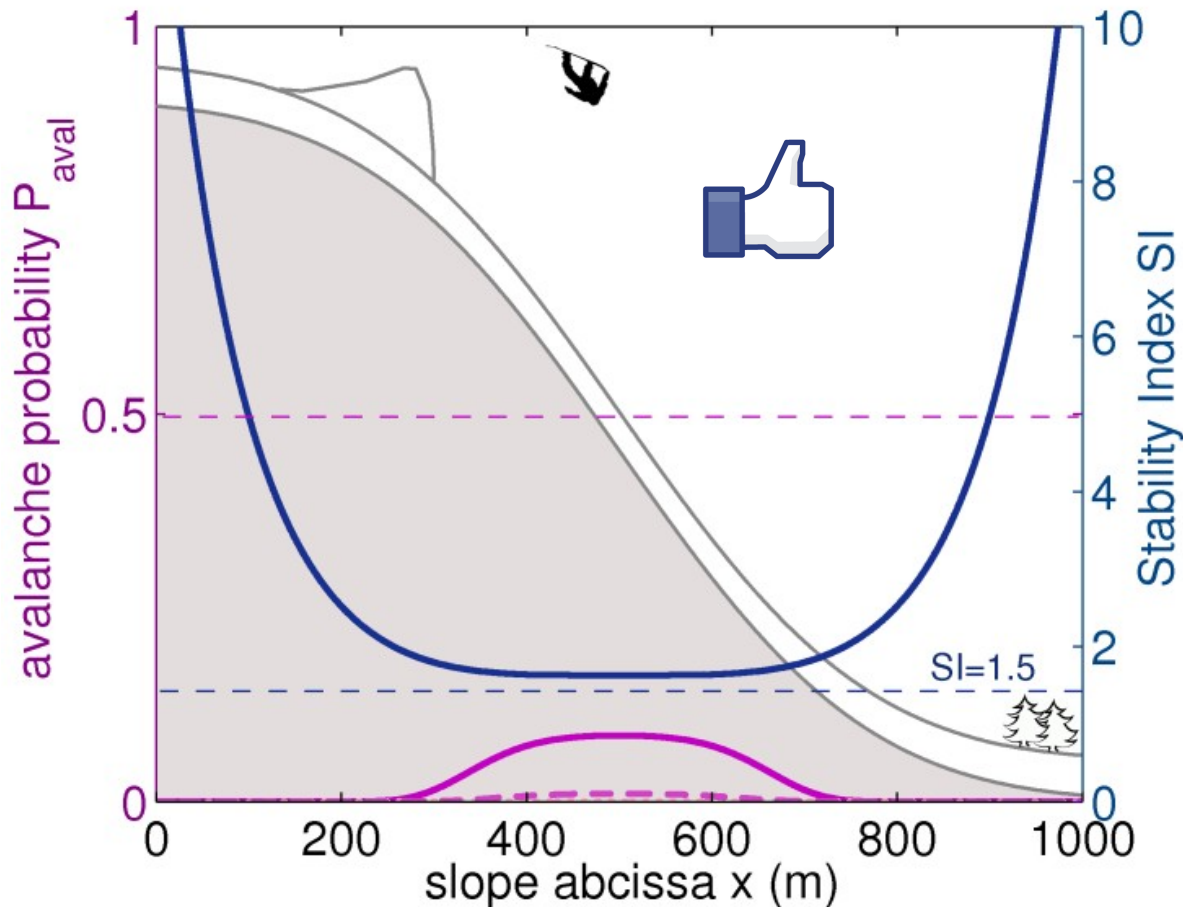
Results

Slope stability evaluation

$hz=50\text{cm}$
 $\rho=250\text{kg/m}^3$
 $E=1\text{MPa}$
 $\tau_p=1000\text{Pa}$

--- CV=0.2
 — CV=0.3

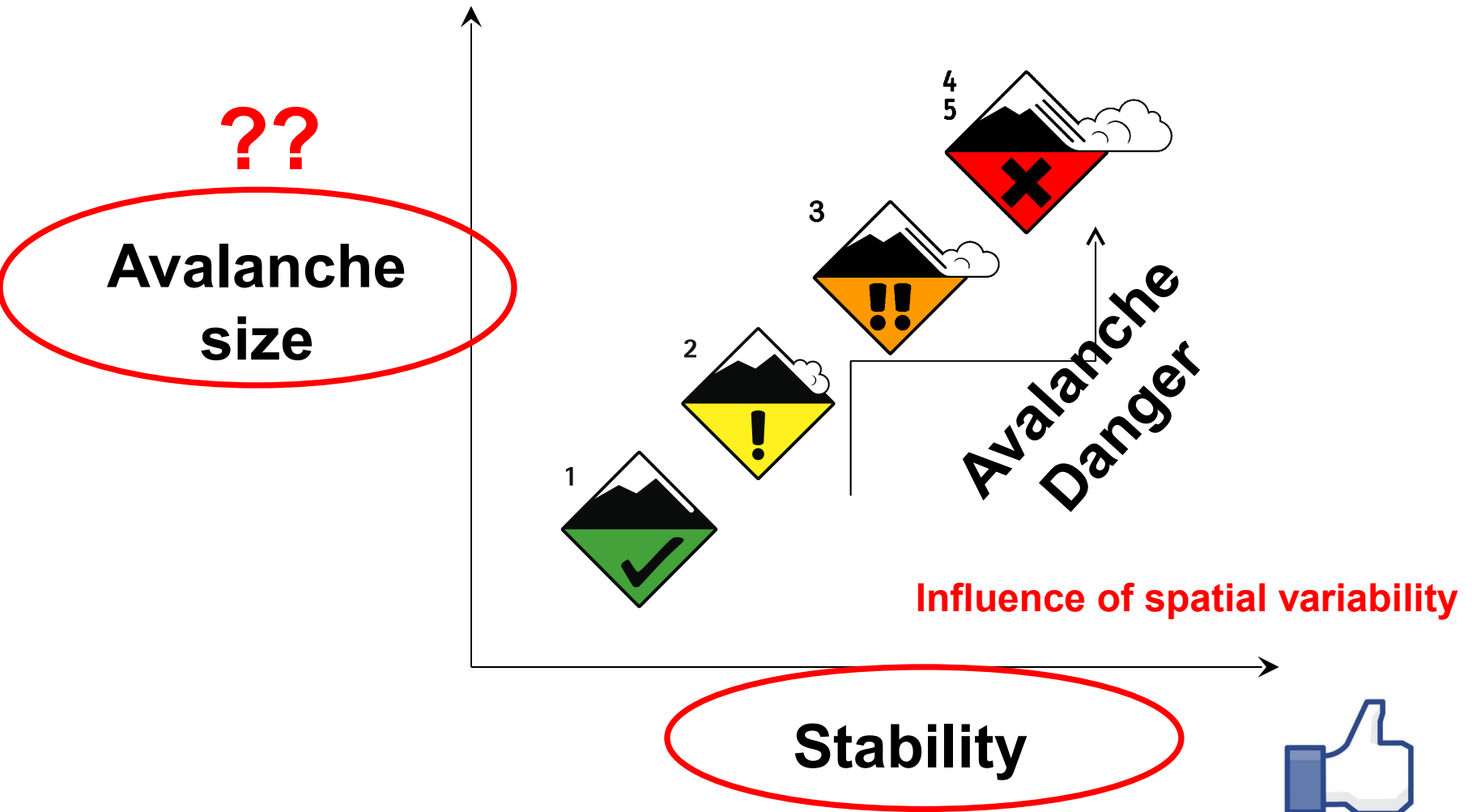
$$CV = \frac{\sigma_{\tau_p}}{\langle \tau_p \rangle}$$



$$\begin{aligned}
 \text{Stability index } SI &= \frac{\text{shear strength}}{\text{shear stress}} \\
 &= \frac{\tau_p}{\tau_{xz}}
 \end{aligned}$$

Objective

Evaluation the size of the release area



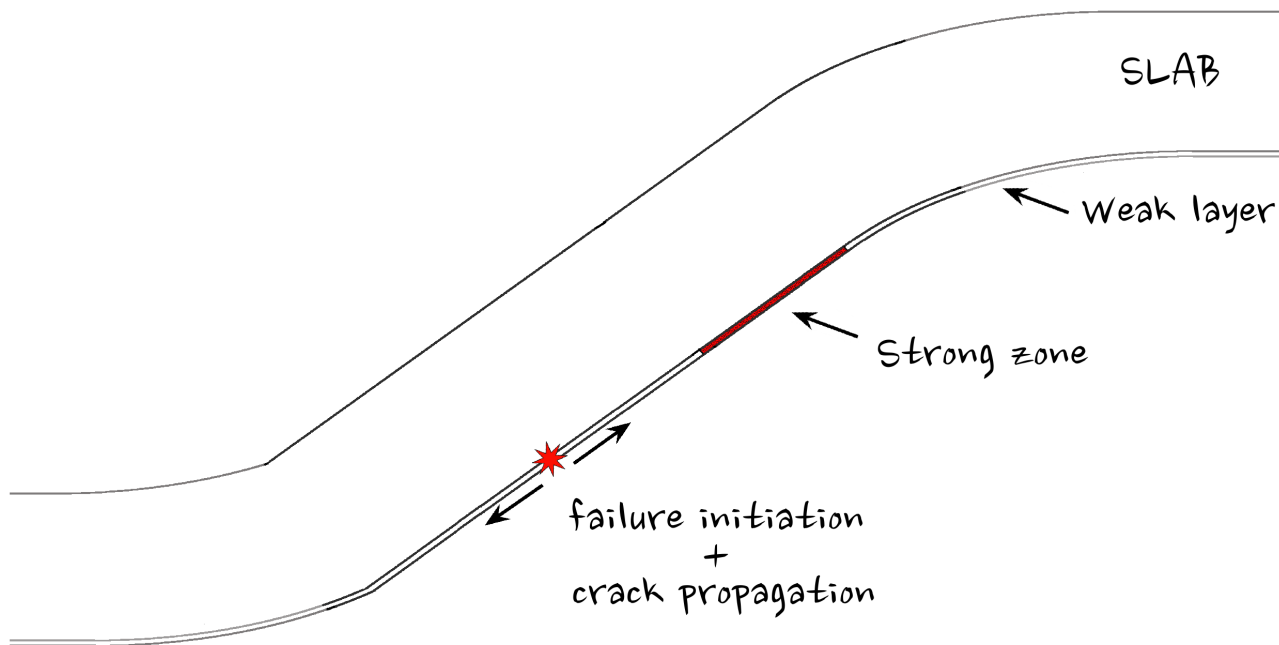
Objective

Answer the question:

Spatial variability of weak layer
shear strength

? possible trigger ?

Slab tensile failure



Objective

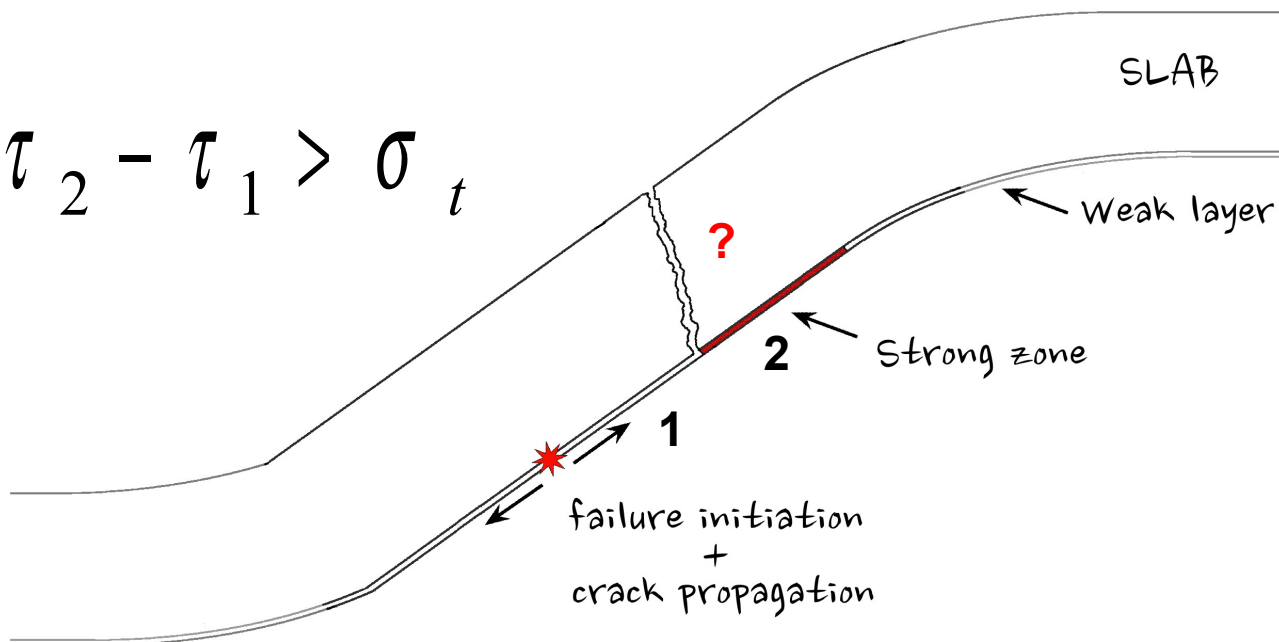
Answer the question:

Spatial variability of weak layer
shear strength

? possible trigger ?

Slab tensile failure

$$\Delta \tau = \tau_2 - \tau_1 > \sigma_t$$



Objective

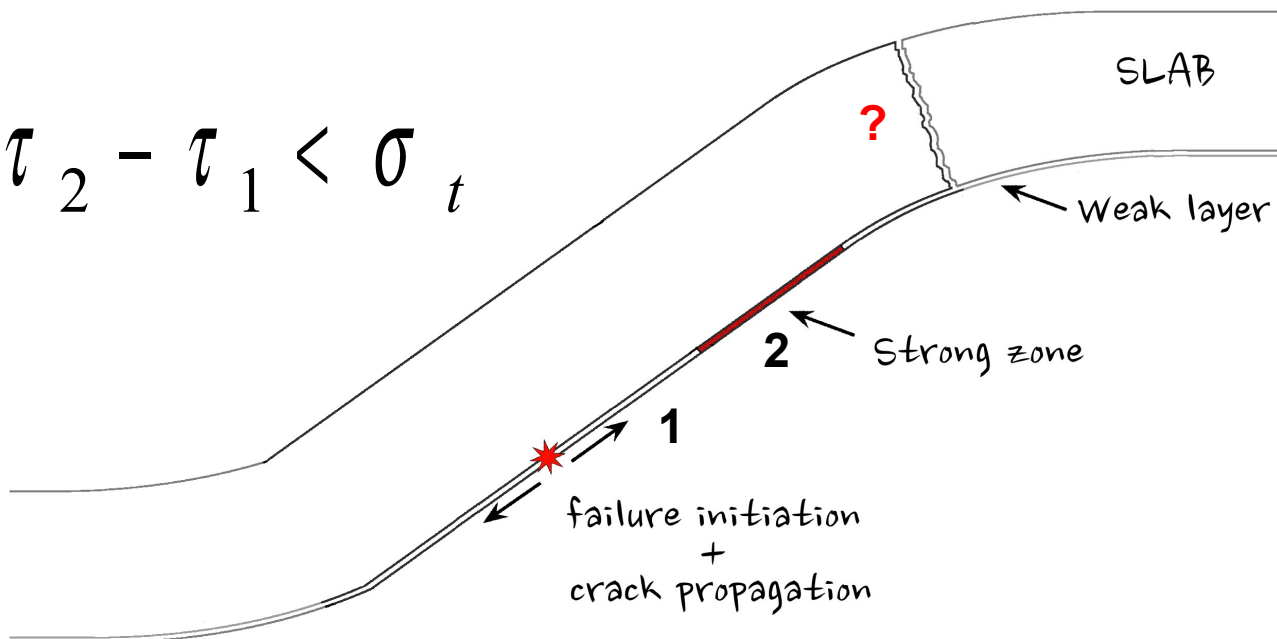
Answer the question:

Spatial variability of weak layer
shear strength

? possible trigger ?

Slab tensile failure

$$\Delta \tau = \tau_2 - \tau_1 < \sigma_t$$



Method

Coupled mechanical - statistical model of slab avalanche release

Same ingredients

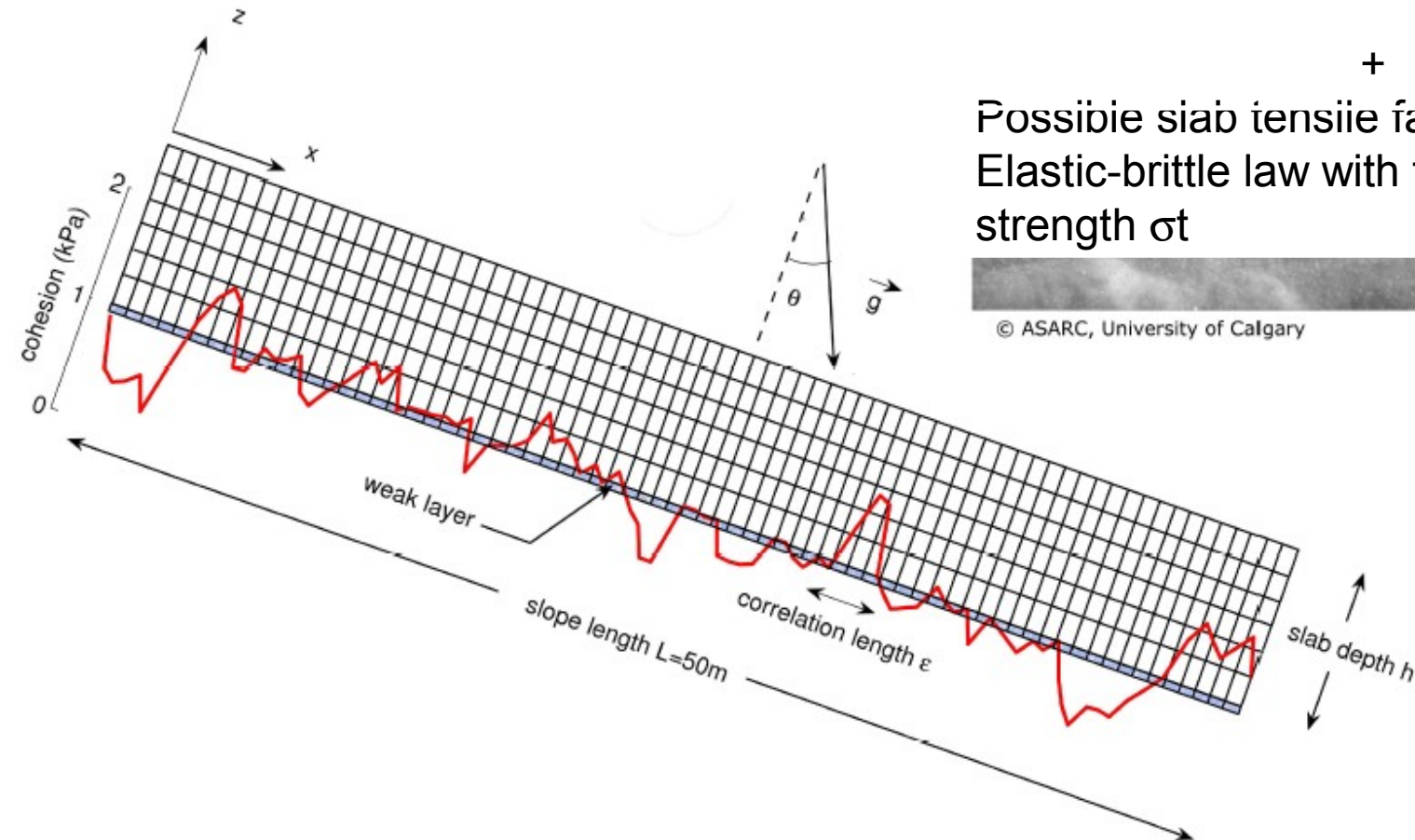
- (1) the spatial variations of WL mechanical properties (shear strength)
- (2) a shear quasi-brittle constitutive law for the WL
- (3) stress redistribution effects by elasticity of the slab

+

Possible slab tensile failure:
Elastic-brittle law with tensile strength σ

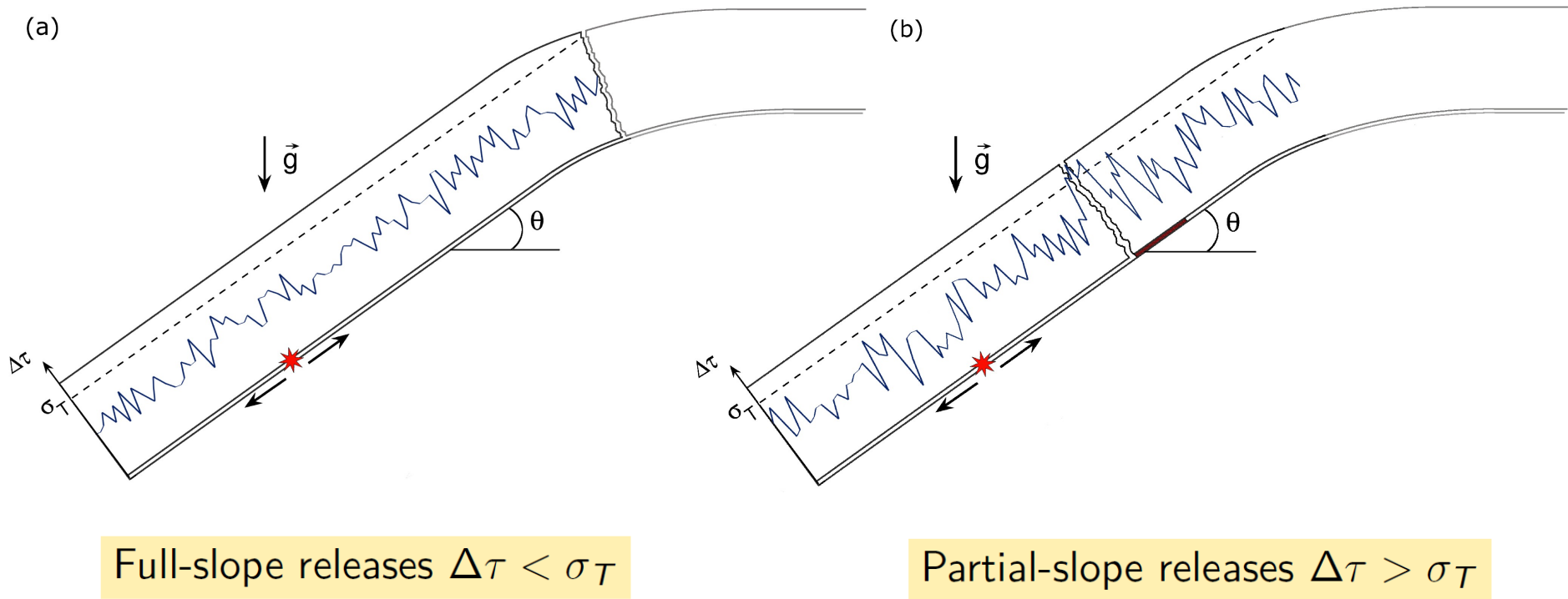


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Results

Two release types

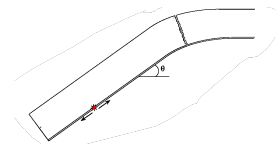
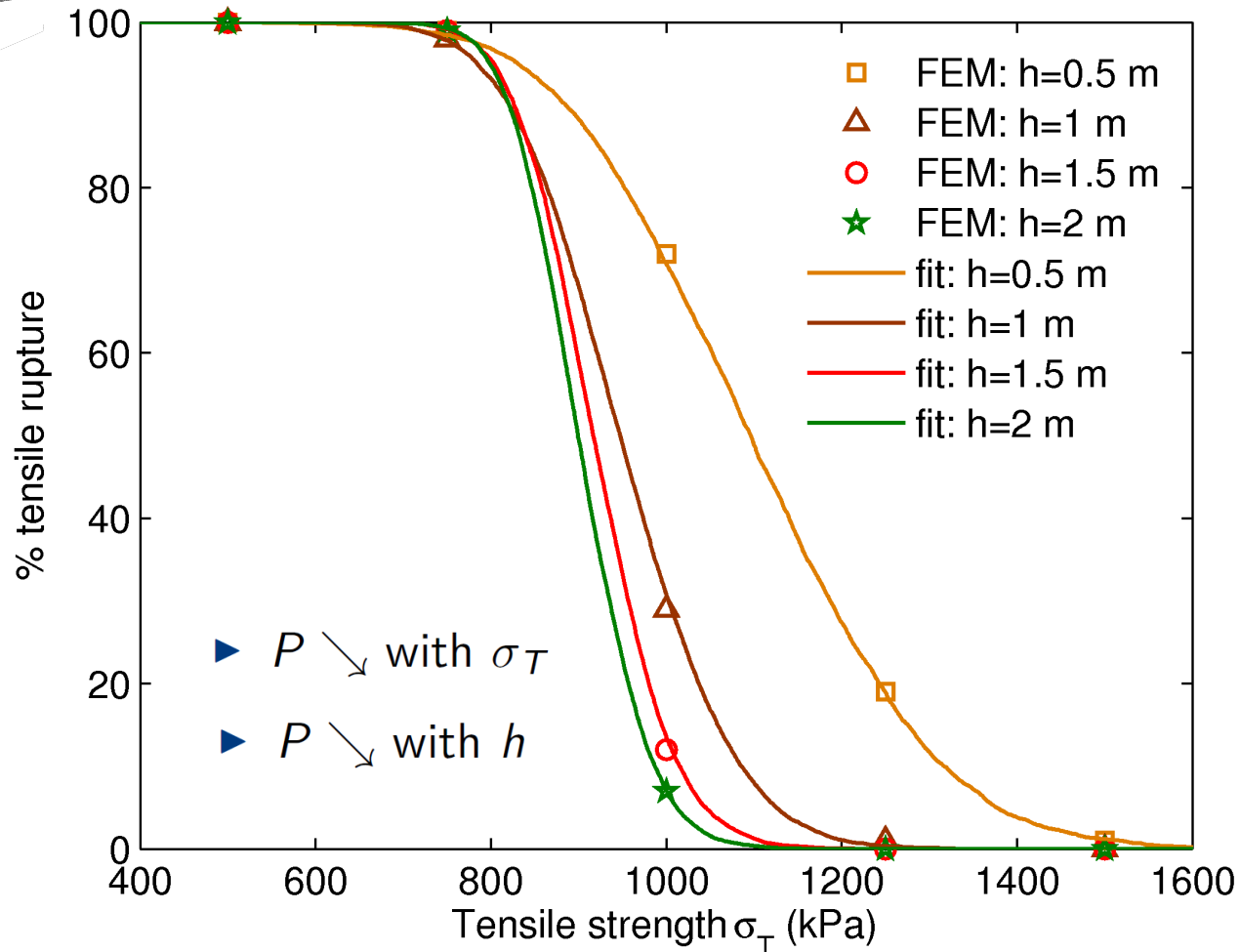
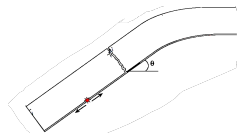


- ▶ The heterogeneity is not sufficient to trigger a tensile failure within the slab
- ▶ The position of the slab tensile failure is influenced by morphological features (rocks, trees, ridge, curvature...).
- ▶ The heterogeneity can trigger a tensile failure within the slab

Results

Proportion between release types

$\rho = 250 \text{ kg/m}^3$
 $E = 1 \text{ MPa}$
 $\langle \tau_p \rangle = 1 \text{ kPa}$
 $CV = 30\%$

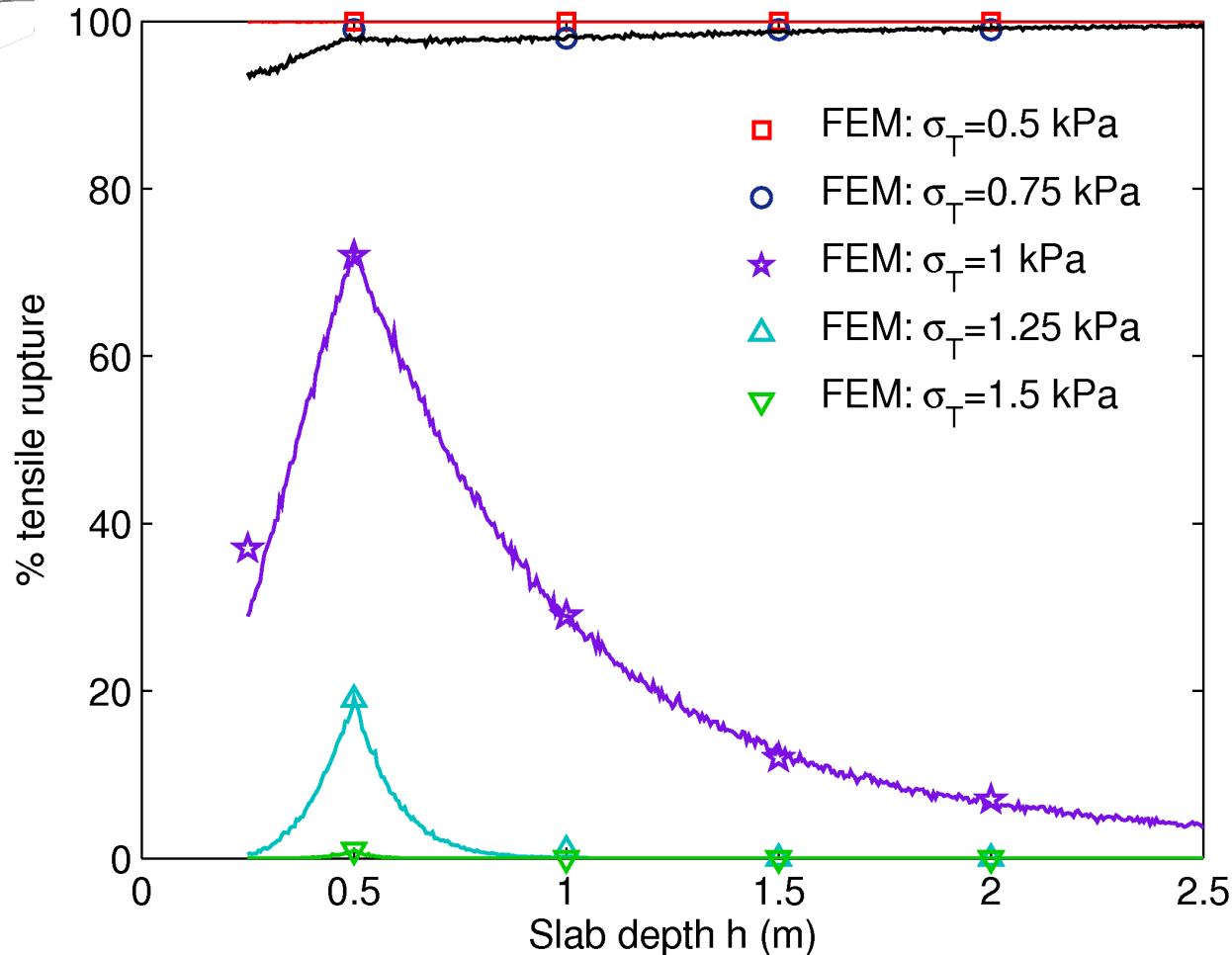
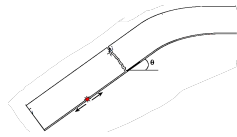


% tensile rupture = % of partial-slope releases = $P(\Delta\tau > \sigma_T)$

Results

Proportion between release types

$\rho = 250 \text{ kg/m}^3$
 $E = 1 \text{ MPa}$
 $\langle \tau_p \rangle = 1 \text{ kPa}$
 $CV = 30\%$

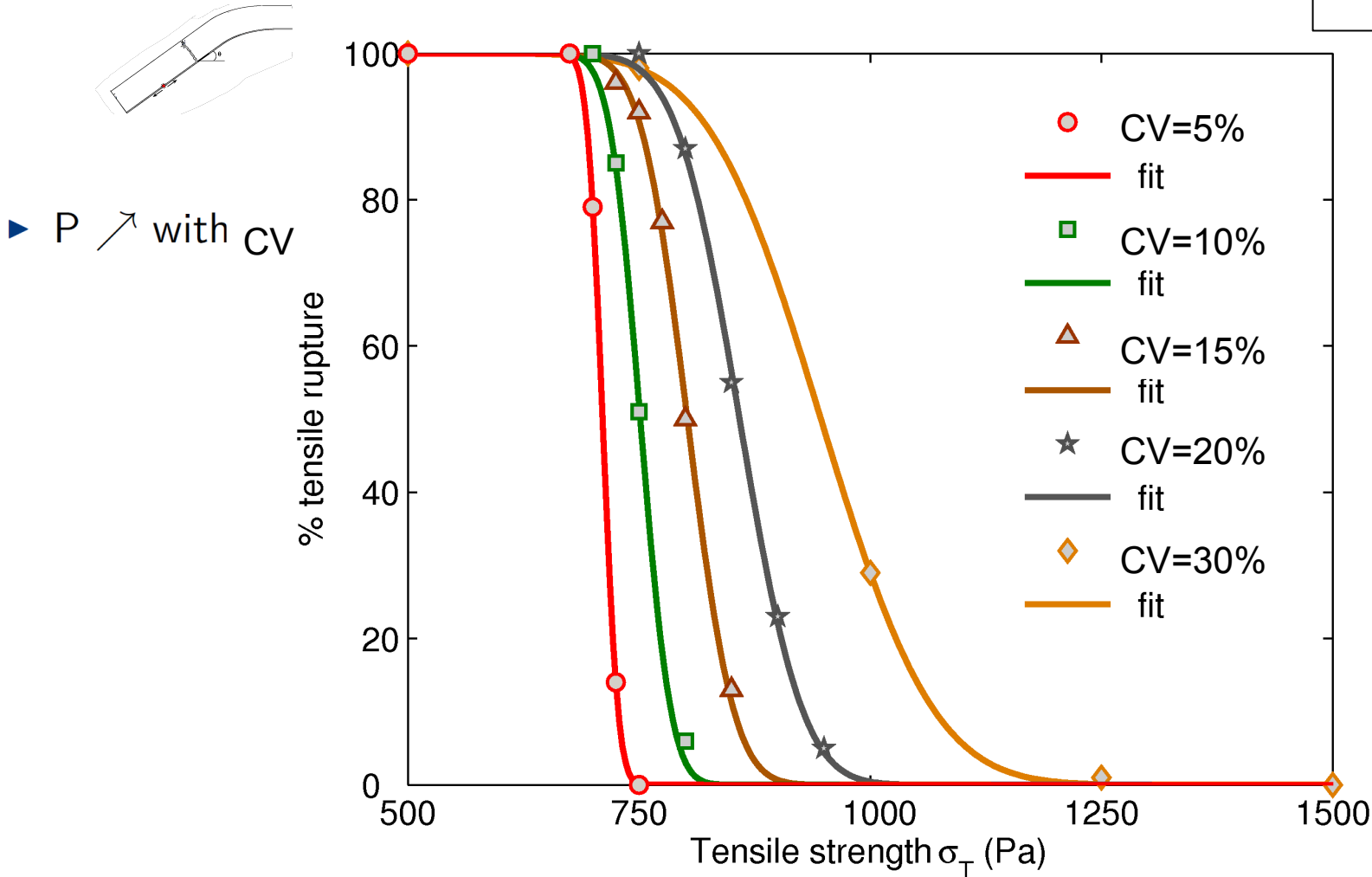


$\% \text{ tensile rupture} = \% \text{ of partial-slope releases} = P(\Delta\tau > \sigma_T)$

Results

Proportion between release types

$\rho = 250 \text{ kg/m}^3$
 $E = 1 \text{ MPa}$
 $\langle \tau_p \rangle = 1 \text{ kPa}$
 $h = 1 \text{ m}$



% tensile rupture = % of partial-slope releases = $P(\Delta\tau > \sigma_T)$

Results

Proportion between release types

$$\begin{aligned}\rho &= 250 \text{ kg/m}^3 \\ \langle \tau_p \rangle &= 1 \text{ kPa} \\ \text{CV} &= 30\% \\ h &= 1 \text{ m}\end{aligned}$$

% tensile rupture

100

80

60

40

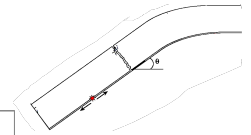
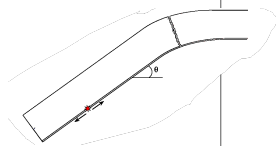
20

0

1

10

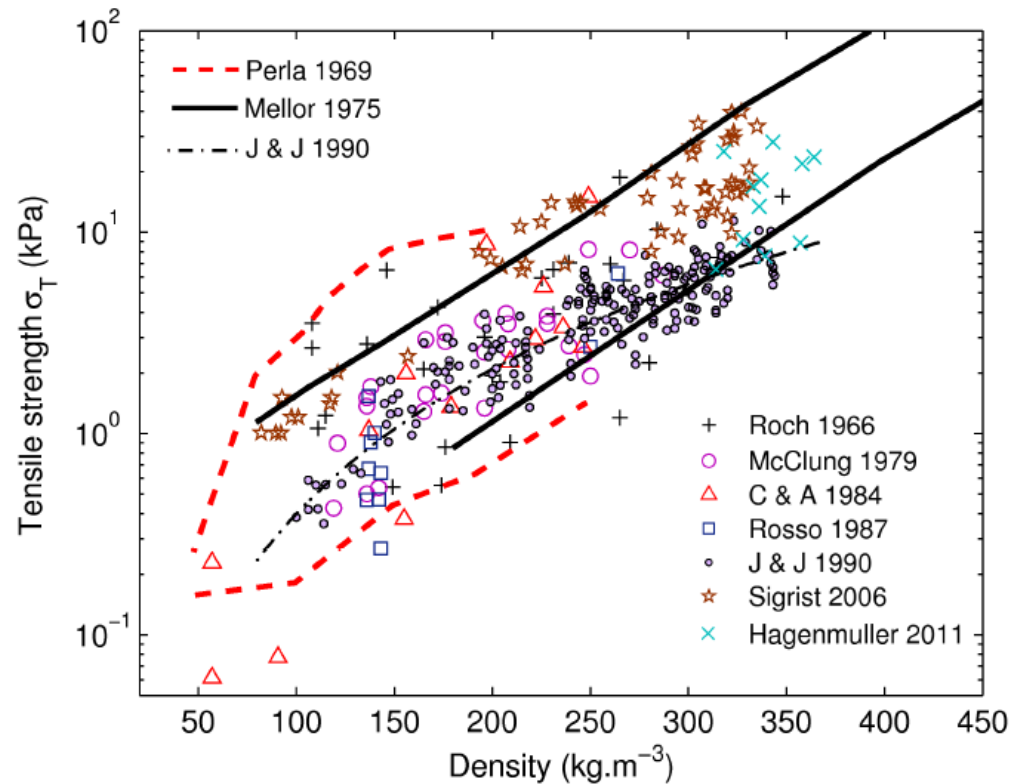
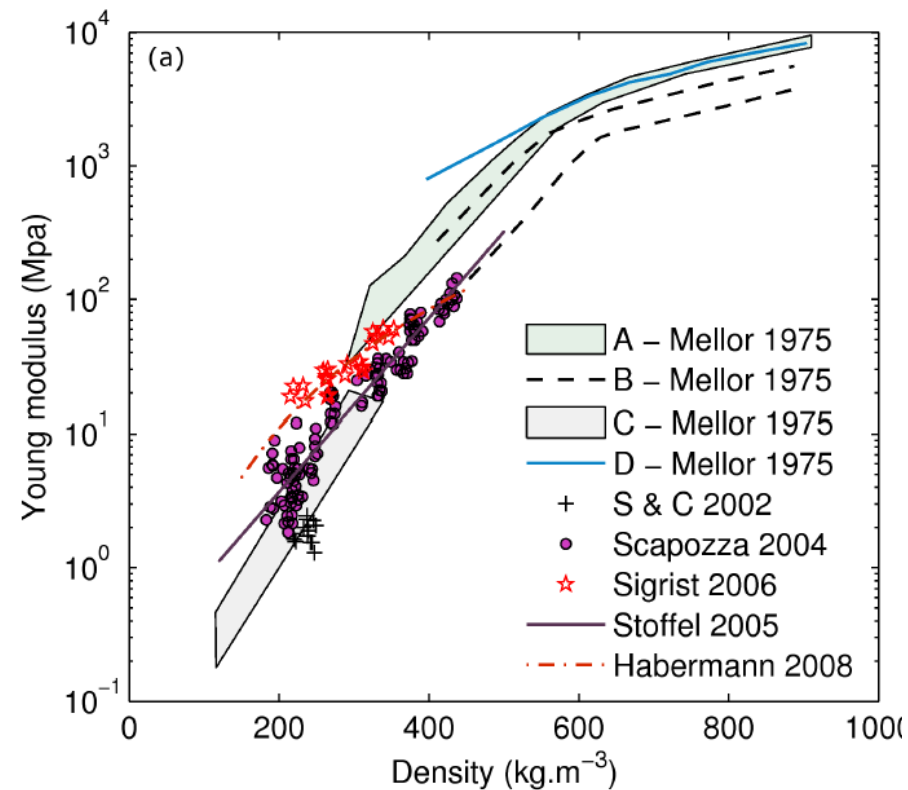
Young's modulus E (MPa)



Interlude

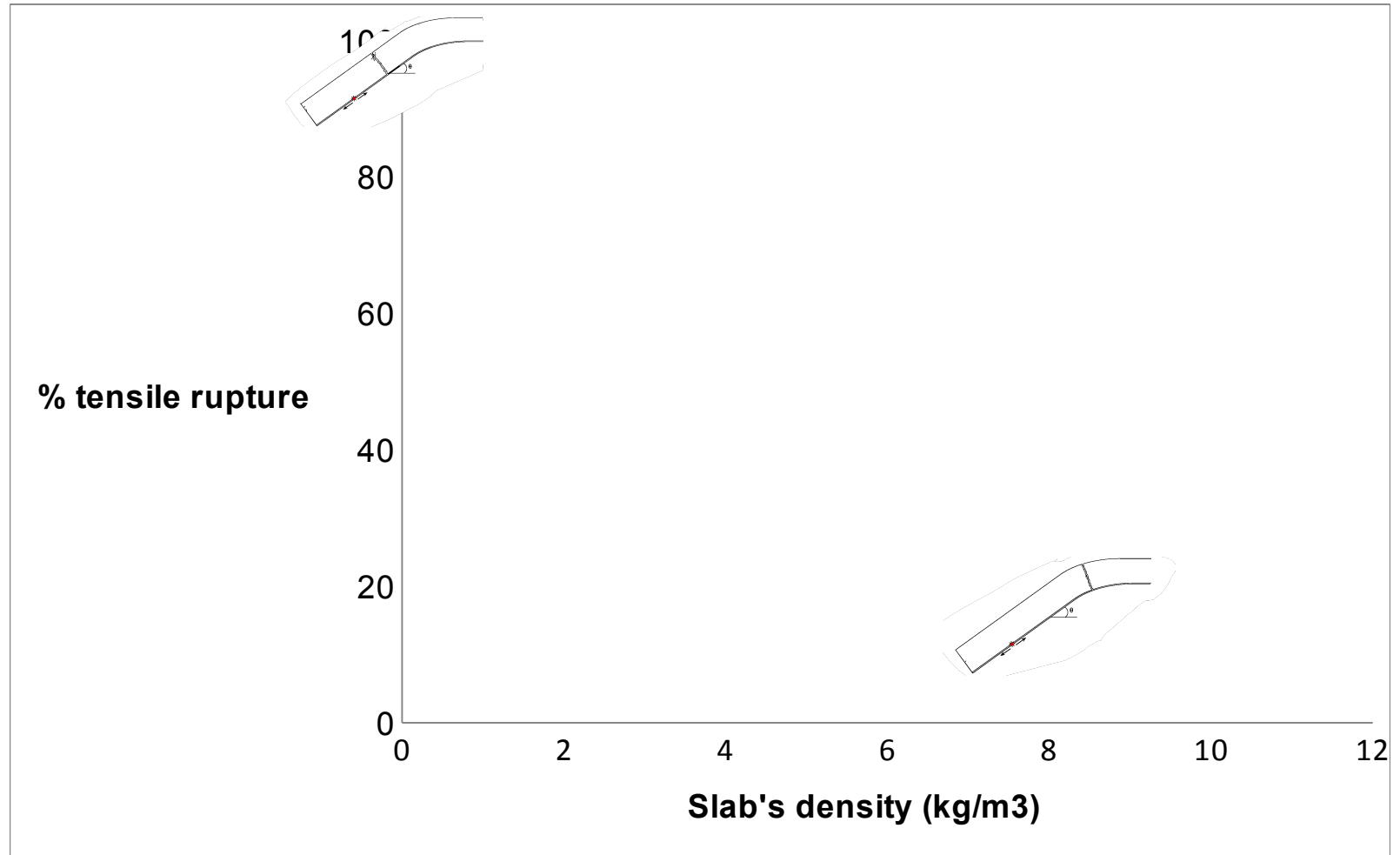
Snow properties

Evolution of Young modulus E and tensile strength σ_t of the slab with density



Back to the results

Using Sigrist (2006)'s evolutions of E and σ_t with ρ



Results

Position of slab's tensile failure

For realistic sets of parameters



The position of the slab tensile failure is influenced by morphological features (rocks, trees, ridge, curvature...)



Conclusions

Mechanical-statistical model of the slab-weak layer system

- the spatial variations of WL mechanical properties (shear strength)
- a shear quasi-brittle constitutive law for the WL
- stress redistribution effects by elasticity of the slab
- slab possible tensile failure

... to study the influence of weak layer shear strength spatial variability

on both

Fracture initiation



Stability



Very important **knock-down effect** on slope stability highlighted

Crack propagation



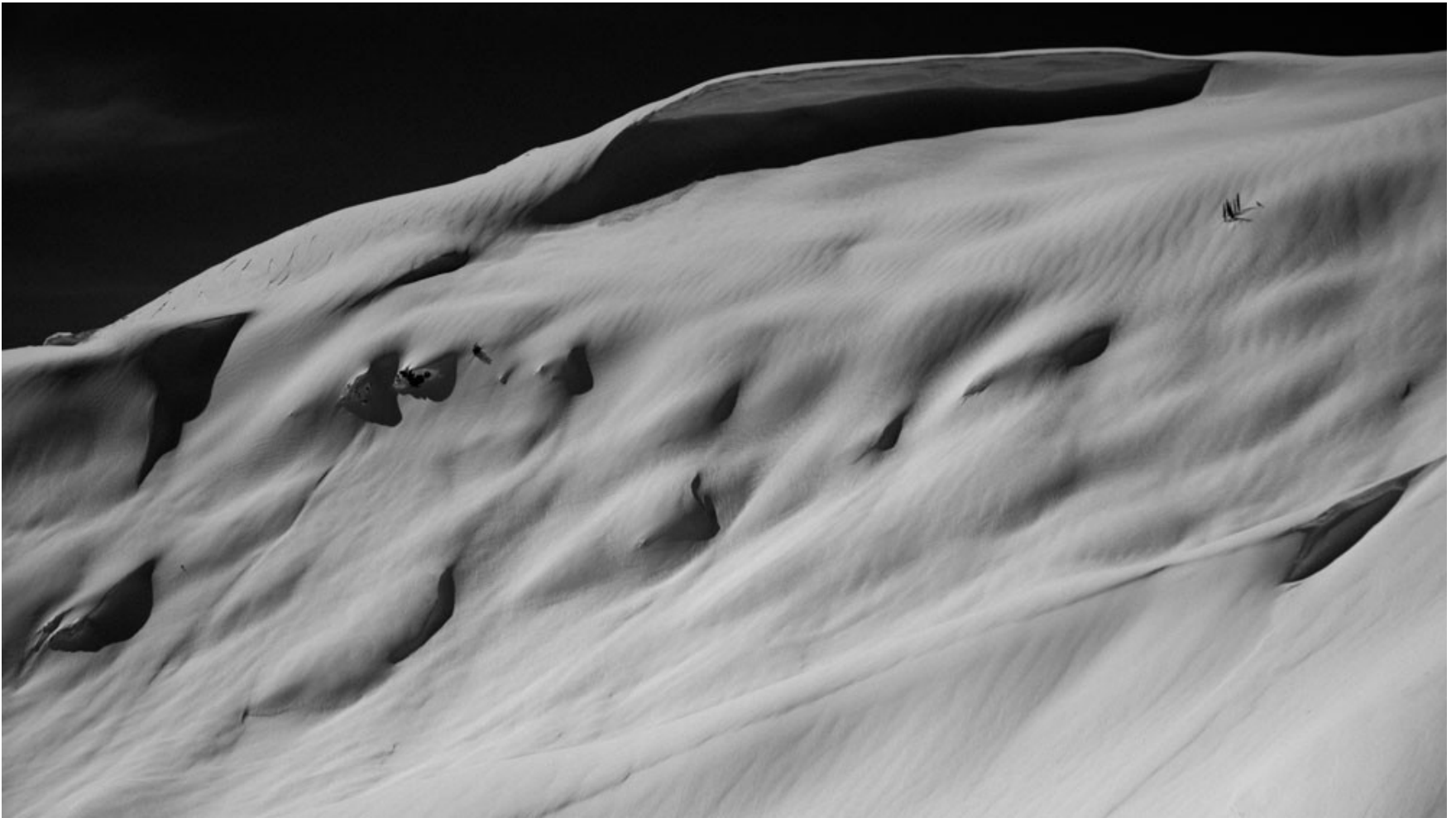
Avalanche size



Major influence of **slope topography** and of the **snow cover distribution**

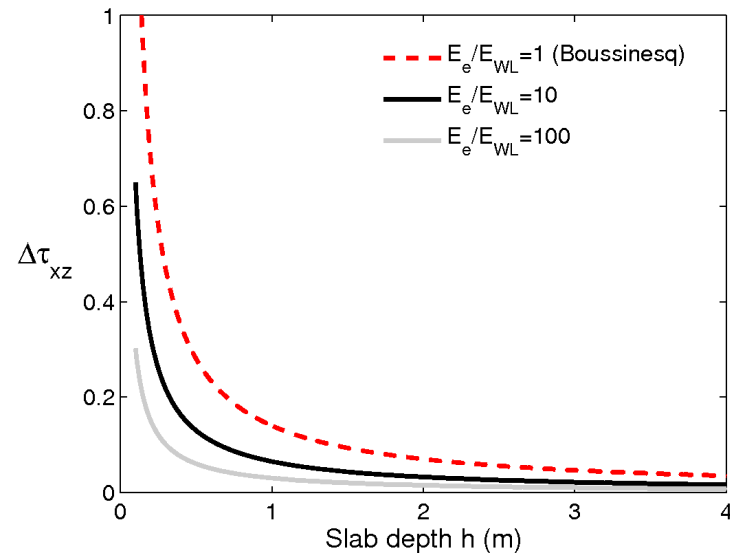
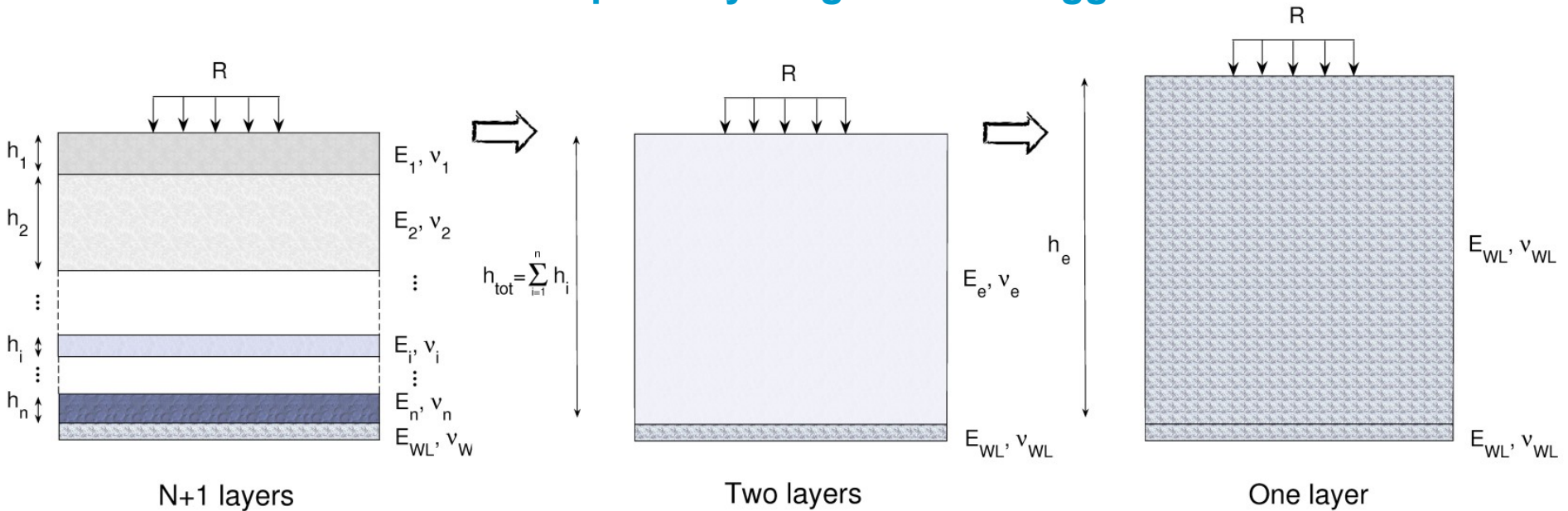
Outlook

Influence of snow cover distribution on avalanche sizes using the same approach



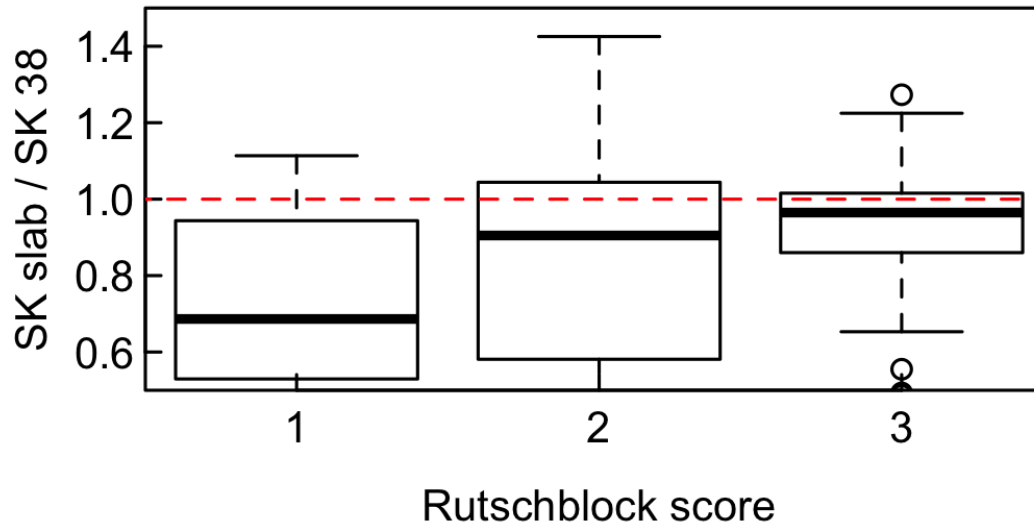
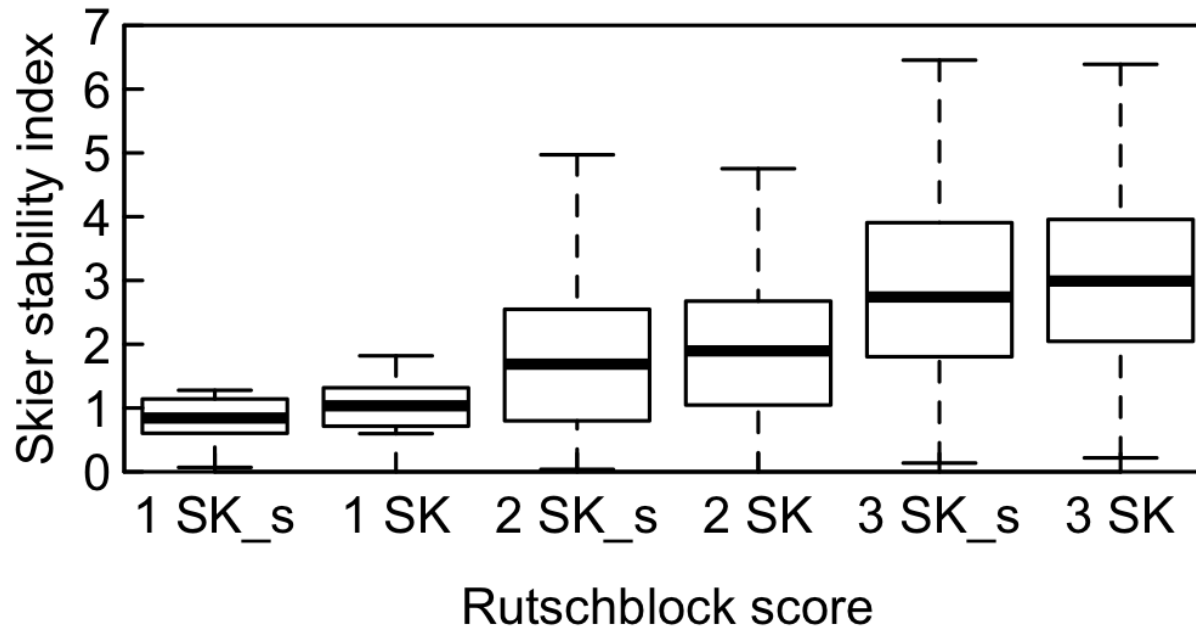
Outlook

Influence of snowpack layering on skier-triggered avalanches



Outlook

Influence of snowpack layering on skier-triggered avalanches



Thanks for your attention!

Do you have any questions?

